Question	Mark Scheme	Marks	
1. (a)	A graph consisting of <u>two distinct sets of vertices</u> X and Y in which arcs can only join a vertex in X to a vertex in Y.	B1 B1	(2)
(b)	A path <u>from an unmatched vertex in X to an unmatched vertex</u> in Y which <u>alternately uses arcs in/not in the matching</u> .	B1 B1	(2)
(c)	The (1-1) matching / pairing of <u>some</u> elements of X with elements of Y.	B1	
(d)	A <u>1-1</u> matching between <u>all</u> elements of X onto Y	B1	(2)
			(6)
2. (a)	Yes, there are <u>no negative</u> values in the <u>profit row</u>	B1	(1)
(b)	$p = 63, x = 0, y = 7, z = 0, r = \frac{9}{2}, s = \frac{2}{3}, t = 0$	M1, A1, A1,	(3)
(c)	$\frac{63}{7} = 9$	M1, A1	(2)
			(6)

Question	Mark Scheme	Marks	
3. (a)	$C_1 = 7 + 14 + 0 + 14 = 35$	B1	
	$C_2 = 7 + 14 + 5 = 26$	B1	
	$C_3 = 8 + 9 + 6 + 8 = 31$	B1	(3)
(b)	Either Min cut = Max flow and we have a flow of 26 and a cut of 26 or C2 is through saturated arcs	B1	(1)
(c)	Using EJ (capacity 5) e. g – will increase flow by 1– ie increase it to 27 since only one more unit can leave E. - BEJL - 1	M1 A1	
	Using FH (capacity 3) e. g will increase flow by 2 – ie increase it can leave F. - BFHJL - 2 Thus choose option 2 add FH capacity 3.	A1	(3) (7)
4. (a)	BD + FG = 1.3 + 0.9 = 2.2 *	M1	(7)
	BF + DG = 1.5 + (1.3 + 0.7) = 3.5	A1	
	BG + DF = 0.7 + (0.9 + 0.8) = 2.4	A1	
	Repeat BD and FG		(3)
	Route e.g. GABC <u>DB</u> FEDBG <u>FG</u>	B1	
	Length = $8.9 + 2.2 = 11.1$ km	M1 A1	(3)
(b)	Only now need to repeat BF of length $1.5 < 2.2$	M1 A1	
	Length = 8.9 +1.5 = 10.4 km saving 0.7 (km)	A1 🔨	(3)
			(9)

Ques	tion	Mark Scheme					Marks		
5.	(a)								
		a	b	c	Integer?	Output list	a = b?		
		90	2	45	Yes	2	No	M1	
		45	2	22.5	No			A1	
		45	3	15	Yes	3	No	A1 🔨	
		15	2	7.5	No			M1	
		15	3	5	Yes	3	No	A1	
		5	2	2.5	No				
		5	3	$1\frac{2}{3}$	No			M1	
		5	5	1	Yes	5	Yes		
					A1	(7)			
	(b)	Gives th	e prime f	actorisati	on of a			B2, 1, 0	(2)
	(c)	C = 1						B1	(1)
									(10)
6.	(a)	<u>See overlay</u>					B1		
								B1	(2)
	(b)	BD, $\left(\frac{A C}{D F}\right)$, BC, Not CD, DE $F \underbrace{-}_{E} \underbrace{-}_{D} C$					M1 A1, A1 B1		
		Length =	= 18 km					B1	(5)
	(c)	DB, DF, BC, CA, DE [5,2,4,1,6,3,]				M1 A1 A1	(3)		
									(10)

Question	Mark Scheme	Marks	
7. (a)	<u>See overlay</u>	B5, 4, 3, 2, 1, 0	(5)
(b)	Either point testing or profit line	M1	
	A $(3\frac{5}{6}, 3\frac{1}{2}) \rightarrow 25\frac{1}{6}$, B $(8\frac{1}{2}, 3\frac{1}{2}) \rightarrow 34\frac{1}{2}$, Accept C $(4,8) \rightarrow 48$ and D $(3,6) \rightarrow 36$		
	Profit line gradient $-\frac{2}{5}$	A1	
	Identifies A $(3\frac{5}{6}, 3\frac{1}{2})$ cost $25\frac{1}{6}$	A1, A1	(4)
(c)	Either point testing or profit line	M1	
	$A(3\frac{5}{6}, 3\frac{1}{2}) \rightarrow \text{not integer so try } (4,4) \rightarrow 20$ Profit line		
	$B(8\frac{1}{2}, 3\frac{1}{2}) \rightarrow \text{not integer so try } (8,4) \rightarrow 32$		
	$\rightarrow \text{try } (7,5) \rightarrow 31 \qquad \qquad \text{gradient} - \frac{3}{2}$		
	Accept C (4,8) $\rightarrow 28$ and D (3,6) $\rightarrow 21$	A1	
	Identifies (8,4) profit 32.	A1 A1	(4) (13)
8. (a)	x = 0, y = 7, z = 9	B1, B1, B1,	(3)
(b)	Length = 22, critical activities B D E L	B1, B1,	(2)
(c) (i)	Float on $N = 22 - 14 - 3 = 5$	B1	
(ii)	Float on $H = 16 - 5 - 3 = 8$	M1 A1	(3)
(d)	<u>See overlay</u>	B4, 3,2,1,0	(4)
(e)	Attempt at 1. e.t. and e.e.t. 22 hours	M1 A1	(2)
			(2) (14)